What it
$$p$$
 Small?
If we can check whether χ good...
• Ren A T times
• Check all of them, return any good
We'll get good χ except $\mu.p$.
 $(1-p)^{T}$
Key fact: $t p \in (0, t)$,
 $t_{f} \leq (1-p)^{k}p \leq \frac{1}{2}$
Thus, $T \gtrsim \frac{1}{p} \log(\frac{1}{2})$
 $\Longrightarrow (1-p)^{T} \leq S$

(hebyshevis meguslity (Port Ull, Section 3.1)

ley players: $\|\lambda[X] := \mathbb{E}[X_5] - \mathbb{E}[X]_5 \le 0$ (convexity) £ (x)² "Sprezo" Story(X) := (Var(X))Aside Variance Crash course Remnder Hour (E: (no creats!!!) $\mathbb{O}\left(\mathcal{C}\left(X\right)\right) = \mathbb{O}\left(\mathcal{C}\left(X\right)\right)$ = (f(X) + (f(Y))= C H(X)

$$\begin{aligned}
\left(\left(\left(X - \left(E(X) \right)^{2} \right)^{2} \right) &= \left(E(X^{2}) \right)^{2} \\
&= 2 \left(\left(X \cdot \left(E(X) \right) \right)^{2} + \left(E(X) \right)^{2} \\
&= \left(E(X^{2}) - \left(E(X) \right)^{2} = \left(V \right)^{2} \right)^{2} \\
&= \left(X^{2} \right)^{2} - \left(E(X) \right)^{2} = \left(V \right)^{2} \\
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&= \left(X^{2} \right$$

Our intuition: for ressource
$$S_{i}$$
,
pick R & Stdev(X)
Mortan's inequality
let r.v. X >D, then $\forall S \in (0,1)$,
 $Pr[X > E(X)] \leq S$
 $e.g. X < ID \in (X)$ except wp. to
 $Proof: if not, let T = E(X)$,
 $E(X) = Pr(X > T) \cdot T + Pr(X < T) \cdot O$
 $> S \cdot T > E(X)$

Chebyshei's hequality) Apply Morkovis with X < (X-E(X)) $\Pr\left(\left(X - \mathbb{E}(X)\right)^2 > \frac{\forall x(X)}{\delta}\right) \leq \delta$ $\iff |X - \mathbb{E}[X]| \ge \frac{Stdev[X]}{\sqrt{5}}$ Thus we have shown except w.p. S, $X \in \left(f(X) - \frac{Stow(X)}{SC}, f(X) + \frac{Stow(X)}{SC} \right)$ R.G. S = Ly (Confidence interval (E(X)-2stder (X), E(X) + 2stder (X)) radius P

Mean / median boosthy (Part VIII, Section 3.2) Ded (: Improve R (mean boosthy) Pecall that R X Story (X) How to halve R? Decrease Var! Basic faut: let X, X2,..., XK inderwart copies of X, $\chi = \frac{1}{2} \sum_{i \in (k)} \chi_i$ $V = \frac{1}{k^2} V \left(\sum_{i \in CK} X_i^{i} \right)$ $=\frac{k^{5}}{k} \ln(\chi) = \frac{k}{k} \ln(\chi)$

Takeowsy: if Ka 121 then our confidence yets 5x better $Vr(\overline{X}) = \zeta Vr(X), \int \zeta^2 X$ for Stoler. 1 des 2: Improve & (medion boosthy) Suppose r.v. X has PC(XEI) Z & for interval ICR (Jahr: let X=median (X1, X2,..., KE) KZ [2log (2) Then, XEI except w.V. S

How to prove?
Step 1: it's enough to show
$$2 \stackrel{k}{\geq} copies \in I$$

e.s. if $k \notin I$ to the night, clarky $< k_2 \notin I$
 $k \leq \frac{1}{2}$ econords
Our gosl: we have contributed that $H = 0.922$; $K = 100$
 $fors K = Cohs_1, 2 \stackrel{k}{\geq} 2 \stackrel{k}{\sim} H$.
Step 2: "Inhomist concertories"
Suppose $i \geq \frac{k}{2}$ copies miss I
 $Pr(2 \stackrel{k}{\leq} 2 \stackrel{k}{\leq} 2 \stackrel{k}{\sim} 2 \stackrel{k}{\leq} 1 \stackrel{k}{\sim} 1 \stackrel{k}$

3-staxe plan:

$$P = 2 \text{ states}(X)$$
, $S = \frac{14}{22}$
 $P = 2 \text{ states}(X)$, $S = \frac{14}{22}$
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Albo:
$$X \leftarrow O_1$$

(aut(): W.p. 2^{-X} , $X \leftarrow X+1$
Pepert(): return $2^{X}-1$
If works ????
Intuition: $X \simeq \log(i+1)$
I

$$\begin{aligned} & 3-\text{step pbn: gives estimate in} \\ & \left((1-\varepsilon)n, (1+\varepsilon)n \right) \quad \forall \cdot p \cdot \mathbf{z} \mid -\mathbf{s} \\ & (NY22): \text{ space } O\left(\log \log \mathbf{s} + \log \frac{1}{2} \right) \\ & Proof of \mathbf{E}: \text{ true when } \mathbf{k} = \mathbf{0} \cdot \left[\log \log \frac{1}{2} + \log \frac{1}{2} \right] \\ & = \sum_{j=0}^{\infty} Pr\left(\mathbf{X}_{k} = j \right) \cdot \left(2^{j} \left(1 - \frac{1}{2^{j}} \right) + 2^{j+1} \binom{1}{2^{j}} \right) \end{aligned}$$

